Tissue P Systems with Cell Division

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Abstract: In tissue P systems several cells (elementary membranes) communicate through symport/antiport rules, thus carrying out a computation. We add to such systems the basic feature of (cell–like) P systems with active membranes – the possibility to divide cells. As expected (as it is the case for P systems with active membranes), in this way we get the possibility to solve computationally hard problems in polynomial time; we illustrate this possibility with SAT problem.

Keywords: Tissue-like P systems, cell division rule, SAT problem, NP-complete problem

1 Introduction

In membrane computing, there are two main classes of P systems: with the membranes arranged hierarchically, inspired from the structure of the cell, and with the membranes placed in the nodes of a graph, all of them at the same level, inspired from the cell inter-communication in tissues. A particularly interesting sub-class of the first class are the systems with active membranes, where the membrane division can be used in order to solve hard problems, e.g., **NP**-complete problems, in polynomial or even linear time, by a space-time trade-off. In the tissue P systems, the communication among cells is performed by means of symport/antiport rules, well-known in biology. Details can be found in [8], [10], as well as in the comprehensive page from the web address http://ppage.psystems.eu).

In this paper we combine the two definitions, and consider tissue P systems (with the communication done through symport/antiport rules) with cell division rules of the same form as in P systems with active membranes, but without using polarizations. The rules are used in the non-deterministic maximally parallel way, with the restriction that if a division rule is used for dividing a cell, then this cell does not participate in any other rule, for division or communication (the intuition is that when dividing, the interaction of the cell with other cells or with the environment is blocked); the cells obtained by division have the same labels as the mother cell, hence the rules to be used for evolving them or their objects are inherited (the label precisely identifies the available rules).

This natural extension of tissue P systems provides the possibility of solving SAT problem in polynomial time (with respect to the number of variables and of clauses), in a confluent way: at precise times, one of the objects yes or no is sent to the environment, giving the answer to the question whether the input propositional formula is satisfiable. The construction is uniform: in a polynomial time, a family of recognizing tissue P systems with cell division is constructed, which, receiving as inputs encodings of instances of SAT, tells us whether or not these instances are satisfiable.

2 Tissue P Systems with Cell Division

We assume the reader to be familiar with basic elements of membrane computing and we directly define the class of P systems which is investigated in this paper.

A tissue P system with cell division of degree $m \ge 1$ is a construct

$$\Pi = (O, E, w_1, \ldots, w_m, R, i_o),$$

where:

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- 1. $m \ge 1$ (the initial degree of the system; the system contains *m* cells, labeled with 1, 2, ..., m; we will use 0 to refer to the environment);
- 2. *O* is the alphabet of *objects*;
- 3. w_1, \ldots, w_m are strings over *O*, describing the *multisets of objects* placed in the *m* cells of the system at the beginning of the computation;
- 4. $E \subseteq O$ is the set of objects present in the environment in arbitrarily many copies each;
- 5. *R* is a finite set of *evolution rules*, of the following forms:
 - (a) (*i*,*x*/*y*, *j*), for *i*, *j* ∈ {0,1,2,...,*m*}, *i* ≠ *j*, and *x*, *y* ∈ *O**; *communication rules*; 1,2,...,*m* identify the cells of the system, 0 is the environment; when applying a rule (*i*,*x*/*y*, *j*), the objects of the multiset represented by *x* are sent from region *i* to region *j* and simultaneously the objects of the multiset *y* are sent from region *j* to region *i*;
 - (b) [a]_i → [b]_i[c]_i, where i ∈ {1,2,...,m} and a, b, c ∈ O; *division rules*; under the influence of object a, the cell with label i is divided in two cells with the same label; in the first copy the object a is replaced by b, in the second copy the object a is replaced by c; all other objects are replicated and copies of them are placed in the two new cells.
- 6. $i_o \in \{1, 2, \dots, m\}$ is the output cell.

Therefore, we use antiport rules for communication (for a rule (i, x/y, j) we say that the maximum of the lengths of x and y is the *weight* of the rule), and division rules as in P systems with active membranes.

The rules of a system as above are used in the non-deterministic maximally parallel manner as customary in membrane computing. In each step, all cells which can evolve must evolve in a maximally parallel way (in each step we apply a multiset of rules which is maximal, no further rule can be added), with the following important mentioning: if a cell is divided, then the division rule is the only one which is applied for that cell in that step, its objects do not evolve by means of communication rules. This is like saying that a cell which divides first cuts all its communication channels with the other cells and with the environment; the dotter cells will participate to the interaction with other cells or with the environment only in the next step – providing that they are not divided once again. Their label precisely identify the rules which can be applied to them.

The computation starts from the initial configuration and proceeds as defined above; only halting computations give a result, and the result is the number of objects present in the halting configuration in cell i_o ; the set of numbers computed in this way by the various halting computations in Π is denoted by $N(\Pi)$.

In the present paper we are not interested in the computing power of systems as above – already systems without membrane division are known to be Turing complete (see [8], [6], etc.), but in their computing efficiency. That is why we introduce a variant of tissue P systems with membrane division, namely *recognizing systems with input* following the definitions of complexity classes in terms of membrane computing (see [9]). Such a system has the form $\Pi = (O, \Sigma, E, w_1, \dots, w_m, R, i_{in})$, where:

- $(O, E, w_1, \dots, w_m, R, 0)$ is a tissue P system with cell division of initial degree $m \ge 1$ (as defined in the previous section, but with the environment, indicated by taking $i_o = 0$, used for reading the output of a computation), and w_1, \dots, w_m are strings over $O - \Sigma$.
- The working alphabet *O* has two distinguished objects yes and no, present in at least one copy in some initial multisets w_1, \ldots, w_m , but not present in \mathcal{E} .
- Σ is an (input) alphabet strictly contained in *O*.
- $i_{in} \in \{1, \ldots, m\}$ is the input cell.

- All computations halt.
- If C is a computation of Π, then either the object yes or the object no (but not both) must have been released into the environment, and only in the last step of the computation.

The computations of the system Π with input $w \in \Sigma^*$ start from a configuration of the form $(w_1, w_2, ..., w_{i_m}w, ..., w_m; E)$, that is, after adding the multiset w to the contents of the input cell i_{in} . We say that the multiset w is *recognized* by Π if and only if the object yes is sent to the environment, in the last step of the corresponding computation. We say that C is an accepting computation (respectively, rejecting computation) if the object yes (respectively, no) appears in the environment associated with the corresponding halting configuration of C.

Definition 1. We say that a decision problem $X = (I_X, \theta_X)$ is solvable in polynomial time by a family $\Pi = {\Pi(n) \mid n \in \mathbb{N}}$ of recognizer tissue-like P systems with cell division if the following holds:

- The family Π is *polynomially uniform* by Turing machines, that is, there exists a deterministic Turing machine working in polynomial time which constructs the system Π(n) from n ∈ N.
- There exists a pair (cod, s) of polynomial-time computable functions over I_X (called a polynomial encoding of I_X in Π) such that:
 - for each instance $u \in I_X$, s(u) is a natural number and cod(u) is an input multiset of the system $\Pi(s(u))$;
 - the family Π is *polynomially bounded* with regard to (X, cod, s), that is, there exists a polynomial function p, such that for each $u \in I_X$ every computation of $\Pi(s(u))$ with input cod(u) is halting and, moreover, it performs at most p(|u|) steps;
 - the family Π is *sound* with regard to (X, cod, s), that is, for each $u \in I_X$, if there exists an accepting computation of $\Pi(s(u))$ with input cod(u), then $\theta_X(u) = 1$;
 - the family Π is *complete* with regard to (X, cod, s), that is, for each $u \in I_X$, if $\theta_X(u) = 1$, then every computation of $\Pi(s(u))$ with input cod(u) is an accepting one.

We denote by PMC_{TD} the set of all decision problems which can be solved by means of recognizer tissue-like P systems with cell division in polynomial time. This class is closed under polynomial-time reduction and under complement.

We close this section with an important remark about the previous way of solving decision problems. Specifically, we have said nothing about the way the computations proceed; in particular, they can be non-deterministic, as standard in membrane computing. It is important however that the systems always stop and always they send out an object which is the correct answer to the input problem. From the soundness and completeness conditions above we deduce that every P system $\Pi(n)$ is *confluent*, in the following sense: every computation of a system with the *same* input multiset must always give the *same* answer.

3 Solving SAT in Polynomial Time

As expected, the possibility to divide cells means the possibility to create an exponential space in a linear time, and this space can be used in order to obtain fast solutions to computationally hard problems.

Theorem 1. *Tissue P systems with active membranes can solve* SAT *in polynomial time. (Otherwise stated,* SAT \in **PMC**_{TD}.)

Proof. Let us consider a propositional formula $\gamma = C_1 \land \dots \land C_m$, consisting of *m* clauses $C_j = y_{j,1} \lor \dots \lor y_{j,k_j}$, $1 \le j \le m$, where $y_{j,i} \in \{x_l, \neg x_l \mid 1 \le l \le n\}$, $1 \le i \le k_j$ (there are used *n* variables). Without loss of generality, we may assume that no clause contains two occurrences of some x_i or two occurrences of some $\neg x_i$ (the formula is not redundant at the level of clauses), or both x_i and $\neg x_i$ (otherwise such a clause is trivially satisfiable, hence can be removed).

We codify γ , which is an instance of SAT with size parameters *n* and *m*, by the multiset

$$cod(\gamma) = \{s_{i,j} \mid y_{j,r} = x_i, \ 1 \le i \le n, 1 \le j \le m, 1 \le r \le k_j\} \\ \cup \{s'_{i,i} \mid y_{j,r} = \neg x_i, \ 1 \le i \le n, 1 \le j \le m, 1 \le r \le k_j\}.$$

(We replace each variable x_i from each clause C_j with $s_{i,j}$ and each negated variable $\neg x_i$ from each clause C_j with $s'_{i,j}$, then we remove all parentheses and connectives. In this way we pass from γ to $cod(\gamma)$ in a number of steps which is linear with respect to $n \cdot m$.)

The instance γ will be processed by the tissue P system $\Pi(s(\gamma))$ with input $cod(\gamma)$, where $s(\gamma) = \langle n, m \rangle = \frac{(n+m)\cdot(n+m+1)}{2} + n$. We construct the recognizing tissue P system (of degree 2) with input

$$\Pi(\langle n,m\rangle) = (O,\Sigma,E,w_1,w_2,R,2),$$

with the following components:

$$\begin{array}{rcl} O &=& \Sigma \cup \{a_i, t_i, f_i \mid 1 \le i \le n\} \cup \{r_i \mid 1 \le i \le m\} \\ &\cup &\{T_i, F_i \mid 1 \le i \le n\} \cup \{T_{i,j}, F_{i,j} \mid 1 \le i \le n, 1 \le j \le m+1\} \\ &\cup &\{b_i \mid 1 \le i \le 3n+m+1\} \cup \{c_i \mid 1 \le i \le n+1\} \\ &\cup &\{d_i \mid 1 \le i \le 3n+nm+m+2\} \cup \{e_i \mid 1 \le i \le 3n+nm+m+4\} \\ &\cup &\{f, g, yes, no\}, \end{array}$$

$$\begin{array}{rcl} \Sigma &=& \{s_{i,j}, s'_{ij} \mid 1 \le i \le n, \ 1 \le j \le m\}, \\ E &=& O - \{yes, no\}, \\ W_1 &=& yes \ no \ b_1 \ c_1 \ d_1 \ e_1, \\ W_2 &=& f \ g \ a_1 \ a_2 \ \dots \ a_n, \end{array}$$

and the following rules.

1. Division rules:

$$[a_i]_2 \to [T_i]_2 [F_i]_2$$
, for all $i = 1, 2, ..., n$.

(Membrane 2 is repeatedly divided, each time expanding one object a_i , corresponding to a variable x_i , into T_i and F_i , corresponding to the values *true* and *false* which this variable may assume. In this way, in *n* steps, we get 2^n cells with label 2, each one containing one of the 2^n truth-assignments possible for the *n* variables. The objects f, g are duplicated, hence a copy of each of them will appear in each cell.)

2. Communication rules:

 $(1,b_i/b_{i+1}^2,0)$, for all i = 1,2,...,n+1, $(1,c_i/c_{i+1}^2,0)$, for all i = 1,2,...,n+1, $(1,d_i/d_{i+1}^2,0)$, for all i = 1,2,...,n+1, $(1,e_i/e_{i+1},0)$, for all i = 1,2,...,3n+nm+m+3.

(In parallel with the operation of dividing cell 2, the counters b_i, c_i, d_i, e_i from cell 1 grow their subscripts. In each step, the number of copies of objects of the first three types is doubled, hence

$$(1, b_{n+1}c_{n+1}/f, 2),$$

 $(1, d_{n+1}/g, 2).$

(In step n + 1, the counters $b_{n+1}, c_{n+1}, d_{n+1}$ are brought in cells with label 2, in exchange of f and g. Because we have 2^n copies of each object of these types and 2^n cells 2, each one containing exactly one copy of f and one of g, due to the maximality of the parallelism of using the rules, each cell 2 gets precisely one copy of each of $b_{n+1}, c_{n+1}, d_{n+1}$. Note that cells 2 cannot divide any more, because the objects a_i were exhausted.)

$$(2, c_{n+1}T_i/c_{n+1}T_{i,1}, 0),$$

$$(2, c_{n+1}F_i/c_{n+1}F_{i,1}, 0), \text{ for each } i = 1, 2, ..., n,$$

$$(2, T_{i,j}/t_iT_{i,j+1}, 0),$$

$$(2, F_{i,j}/f_iF_{i,j+1}, 0), \text{ for each } i = 1, 2, ..., n \text{ and } j = 1, 2, ..., m$$

(In the presence of c_{n+1} , the objects T_i , F_i introduce the objects $T_{i,1}$ and $F_{i,1}$, respectively, which initiates the possibility of introducing *m* copies of each t_i and f_i in each cell 2. The idea is that because we have *m* clauses, in order to check their values for a given truth-assignment of variables, it is possible to need one value for each variable for each clause. Note that this phase needs 2n steps for introducing the double-subscripted objects $T_{i,1}$, $F_{i,1}$ – for each one we need one step, because we have only one copy of c_{n+1} available – then further *m* steps are necessary for each $T_{i,1}$, $F_{i,1}$ to grow its second subscript; all these steps are done in parallel, but for the last introduced $T_{i,1}$, $F_{i,1}$ we have to continue *m* steps after the 2n necessary for priming. In total, we perform 2n + m steps.)

$$(2, b_i/b_{i+1}, 0),$$

 $(2, d_i/d_{i+1}, 0),$ for all $i = n+1, \dots, (n+1) + (2n+m) - 1$

(In parallel with the previous operations, the counters b_i and d_i increase their subscripts, until reaching the value 3n + m + 1. This is done in all cells 2 at the same time. Simultaneously, e_i increases its subscript in cell 1.)

$$(2, b_{3n+m+1}t_is_{i,j}/b_{3n+m+1}r_j, 0), (2, b_{3n+m+1}f_is'_{i,j}/b_{3n+m+1}r_j, 0), \text{ for all } 1 \le i \le n \text{ and } 1 \le j \le m, (2, d_i/d_{i+1}, 0), \text{ for all } i = 3n+m+1, \dots, (3n+m+1)+nm-1.$$

(In the presence of b_{3n+m+1} – and not before – we check the values assumed by clauses for the truth-assignments from each cell 2. We have only one copy of b_{3n+m+1} in each cell, hence we need at most *nm* steps for this: each clause contains at most *n* literals, and we have *m* clauses. In parallel, *d* increases the subscript, until reaching the value 3n + nm + m + 1.)

 $(2, d_{3n+nm+m+i}r_i/d_{3n+nm+m+i+1}, 0)$, for all i = 1, 2, ..., m.

(In each cell with label 2 we check whether or not all clauses are satisfied by the corresponding truth-assignment. For each clause which is satisfied, we increase by one the subscript of d, hence the subscript reaches the value 3n + nm + 2m + 1 if and only if all clauses are satisfied.)

$$(2, d_{3n+nm+2m+1}/f \text{ yes}, 1).$$

(If one of the truth-assignments from a cell 2 has satisfied all clauses, then we reach $d_{3n+nm+2m+1}$, which is sent to cell 1 in exchange of the objects yes and f.)

 $(2, yes/\lambda, 0).$

(In the next step, the object yes leaves the system, signaling the fact that the formula is satisfiable. In cell 1, the counter e will increase one more step its subscript, but after that it will remain unchanged – it can leave cell 1 only in the presence of f, but this object was already moved to cell 2.)

 $(1, e_{3n+nm+2m+2}f \operatorname{no}/\lambda, 2),$ $(2, \operatorname{no}/\lambda, 0).$

(If the counter *e* reaches the subscript 3n + nm + 2m + 2 and the object *f* is still in cell 1, then the object no can be moved to a cell 2, randomly chosen, and from here it exits the system, signaling that the formula is not satisfiable.)

In order to show that the family $\Pi = \{\Pi(\langle n, m \rangle) \mid n, m \in \mathbb{N}\}\$ is polynomially uniform by deterministic Turing machines we first note that the sets of rules associated with the system $\Pi(\langle n, m \rangle)$ are recursive. Hence, it is enough to note that the amount of necessary resources for defining each system is quadratic in max $\{n, m\}$, and this is indeed the case, since those resources are the following:

- 1. Size of the alphabet: $6nm + 17n + 4m + 12 \in \Theta(nm)$.
- 2. Initial number of cells: $2 \in \Theta(1)$.
- 3. Initial number of objects: $n + 8 \in \Theta(n)$.
- 4. Number of rules: $4nm + 10n + 3m + 16 \in \Theta(nm)$.
- 5. Upper bound for the length of the rules: $3 \in \Theta(1)$

From the previous explanations, one can see that, starting with the multiset $cod(\gamma)$ added to cell 2, which is the input cell, the system correctly answers the question whether or not γ is satisfiable. The duration of the computation is polynomial in terms of *n* and *m*: the answer yes is sent out in step 3n + nm + 2m + 2, while the answer no is sent out in step 3n + nm + 2m + 4. This concludes the proof.

The antiport rules from the previous construction are of weight at most 3, but the weight can be reduced to two, at the expense of some slowdown of the system. For instance, instead of the rule $(1, e_{3n+nm+2m+2}f \text{ no}/\lambda, 2)$ we can consider the rules $(1, e_{3n+nm+2m+2}f/h, 0)$, $(1, h \text{ no}/\lambda, 2)$, where *h* is a new object. We can proceed in the same way with the rules $(2, b_{3n+m+1}t_is_{i,j}/b_{3n+m+1}r_j, 0)$,

 $(2, b_{3n+m+1}f_is'_{i,j}/b_{3n+m+1}r_j, 0)$, for $1 \le i \le n$ and $1 \le j \le m$, but in this way instead of at most *nm* steps for finding the satisfied clauses we will need at most 2nm steps. The details are left to the reader.

Taking into account that SAT is an **NP**-complete problem and the class PMC_{TD} is closed under polynomial-time reduction and under complement, we have:

Corollary 2. NP \cup **co-**NP \subseteq **PMC**_{TD}

4 Final Remarks

We have proven that by adding the membrane division feature to tissue P systems (with the communication done by antiport rules of a small weight) we can solve **NP**-complete problems in polynomial time. We exemplify this possibility with SAT problem.

It remains as a research topic to consider the same extension for other types of systems, for instance, for cell P systems with symport/antiport rules, or for neural P systems (with states associated with cells and multiset rewriting rules for processing the objects. The difficulty in the case of cell P systems with symport/antiport comes from the fact that only the skin membrane can communicate with the environment; on the other hand, the skin membrane cannot be divided, hence we need exponentially many objects for communication with inner membranes, and such objects should be brought in from the environment. In turn, neural P systems with the maximal use of rules and replicated communication are already known to be able to solve **NP**-complete problems in polynomial time; the challenge now is not to use replication). In spite of these difficulties, we expect results similar to the above one also in these cases.

Another problem which remains open is to consider tissue P systems with the communication using only symport rules.

A previous version of the present paper was circulated in the volume of the Second Brainstorming Week on Membrane Computing, held in Sevilla, in February 2004, and in the meantime several papers have considered tissue-like P systems with cell division as a framework for devising polynomial solutions to **NP**-complete problems. For instance, [2] deals with the Subset Sum problem, [3] deals with the Partition problem, [5] deals with the Vertex Cover problem, and [4] considers the 3–coloring problem. What is not yet investigated is the possibility to also solve **PSPACE** problems, as it is the case, for instance, for cell-like P systems with division of non-elementary membranes (see [11]) or with membrane creation (see [7]). This last possibility for producing working space, cell creation rules, has been only recently considered for tissue P systems [1]. Let us recall that this kind of rules does not perform replication of objects, as it happens with cell-division rules, and it is an open question whether tissue P systems with communication and membrane creation rules can solve efficiently computationally hard problems.

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